## Math Virtual Learning

## College Prep Algebra

April 15, 2020

College Prep Algebra Lesson: April 15, 2020

## Objective/Learning Target:

Students will use the Change-of-Base formula to evaluate logarithmic expressions.

## Let's get started:

If you can, find a basic scientific calculator like the one pictured here. How would you enter $\log _{5}(12)$ when the only keys you have are LOG and LN?


Lesson:
Mathematicians had the same question-only they didn't have calculators, they had Base 10 log charts (LOG) and Base e log charts (LN).

Watch this video for this really simple solution to the question

- What is $\log _{4}(17)$ when you only have LOG or LN on your calculator?

This formula is known as the

## Change-of-Base formula.

Here is a picture of it from the textbook "College Algebra, 3rd Edition" by Cynthia Young, page 517

Notice you can use the LOG key or the LN key

## CHANGE-OF-BASE FORMULA

For any logarithmic bases $a$ and $b$ and any positive number $M$, the change-of-base formula says that

$$
\log _{b} M=\frac{\log _{a} M}{\log _{a} b}
$$

In the special case when $a$ is either 10 or $e$, this relationship becomes

$$
\begin{array}{cc}
\text { Common Logarithms } & \text { Natural Logarithms } \\
\qquad \log _{b} M=\frac{\log M}{\log b} & \text { or } \\
\log _{b} M=\frac{\ln M}{\ln b}
\end{array}
$$

It does not matter what base we select ( $10, e$, or any other base), the ratio will be the same.

## Practice:

To practice the Change-of-Base formula, use the worksheet link and the scientific calculator link below.

## Change of base practice AND answer key

 Scientific Calculator
## Additional Practice

# Khan Academy Online Practice Problems 

IXL free online practice: ONLY USE FORMULA WITH LOG

